

**A criterion for (non-)planarity of the transformation graph  $G^{xyz}$  when  $xyz = - + +$**

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**Abstract**

The transformation graph  $G^{-++}$  of  $G$  is the graph with vertex set  $V(G) \cup E(G)$  in which the vertex  $x$  and  $y$  are joined by an edge if one of the following conditions holds: (i)  $x, y \in V(G)$  and  $x$  and  $y$  are not adjacent in  $G$ , (ii)  $x, y \in E(G)$  and  $x$  and  $y$  are adjacent in  $G$ , (iii) one of  $x$  and  $y$  is in  $V(G)$  and the other is in  $E(G)$ , and they are incident in  $G$ . In this paper we present characterizations of graphs whose transformation graphs  $G^{-++}$  are eulerian, outerplanar, maximal outerplanar or minimally nonouterplanar. Further we establish a necessary and sufficient condition for the transformation graphs  $G^{-++}$  to have crossing number one or two.

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