

## Further results on super mean graphs

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### Abstract

Let  $G$  be a graph and  $f : V(G) \rightarrow \{1, 2, 3, \dots, p + q\}$  be an injection. For each edge  $e = uv$ , the induced edge labeling  $f^*$  is defined as follows:

$$f^*(e) = \begin{cases} \frac{f(u) + f(v)}{2} & \text{if } f(u) + f(v) \text{ is even.} \\ \frac{f(u) + f(v) + 1}{2} & \text{if } f(u) + f(v) \text{ is odd.} \end{cases}$$

Then  $f$  is called super mean labeling if  $f(V(G)) \cup \{f^*(e) : e \in E(G)\} = \{1, 2, 3, \dots, p + q\}$ . A graph that admits a super mean labeling is called super mean graph. In this paper we study the super meanness of subdivision graph of  $K_{1,3}$ , super meanness of  $P_{\tau,4}$ , super meanness of some caterpillars and super meanness of some duplicate graphs.

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